#### **Augmented Heat Transfer Surface**

#### **Concept**

Develop a low pumping power augmented surface based on experimentally and mathematically based optimization of surface roughness or concavities.

#### **Project Goals**

Design, Test, and implement an experimentally and numerically optimized thermal heat sink that for heat removal from the heatpipes and microchips.

#### **Approach**

Develop optimized volumetric heat dissipation device (VHDD) for surface heatflux removal based on the heterogeneous scaled VAT approach. In order to accomplish this, numerical optimization and a literature survey will be performed in order to predict several candidate VHDD. These heat sinks will be individually tested of heat transfer and flow resistance characteristics. The experiemntal and numerical dta will be used to optimize the physical parameters to obtain an optimal heat sinkfor system design and testing.

# **Heat Sink Optimization Procedures**



## **Heat Sink Model**



## **Heat Sink Optimization**

## **Optimization goal: Maximize Heat sink Effectiveness Heat sink effectiveness evaluation**

• Pumping power per unit volume

$$P_{p} = \frac{P}{\Omega} = \frac{\dot{m}\,\Delta p}{\rho_{f}\Omega} = f_{f}\,\operatorname{Re}_{por}^{3}\langle m_{yz}\rangle \left(\frac{\overset{*}{s}\overset{4}{all}}{\langle m\rangle^{4}}\right) \frac{\mu^{3}}{128\rho_{f}^{2}} \left[\frac{W}{m^{3}}\right] \qquad f_{f} = \left[\frac{2\langle m\rangle\,\Delta p}{\rho_{f}\tilde{U}^{2}s_{all}^{*}L_{x}}\right]$$

• Heat transfer rate per unit volume

$$H_{r} = \frac{S_{b}\alpha_{w}^{*}}{\Omega} = Nu_{b} \frac{k_{f}S_{all}^{*}}{4\langle m \rangle}S_{b}^{*}, \left[\frac{W}{m^{3}K}\right] \qquad \qquad Nu_{b} = \frac{q_{w}d_{por}}{\left(T_{b} - T_{in}\right)k_{f}}$$

• Heat sink heterogeneous effectiveness

$$E_{eff-het} = \frac{H_r}{P_p} = \left[\frac{Nu_b}{f_f \operatorname{Re}_{por}^3} \left(32\frac{s_b^*}{\langle m_{yz}\rangle}\frac{\langle m\rangle^3}{s_{all}^{*3}}\right)\frac{k_f \rho_f^2}{\mu^3}\right], \quad \left[\frac{1}{K}\right],$$

# **VAT Control Equations**

#### **MOMENTUM EQUATION**

$$\frac{\partial}{\partial z^*} \left( L_{M4N} \frac{\partial \widetilde{\overline{u}} (z^*)^*}{\partial z^*} \right) + U_{MConv} + U_{MFriction} - U_{MDrag} = \frac{1}{m_0}$$

### **ENERGY EQUATION IN THE FLUID PHASE**

$$\widetilde{\overline{u}}^{*} \frac{\partial \widetilde{T}^{*}(x^{*}, z^{*})}{\partial x^{*}} = \frac{\partial}{\partial z^{*}} \left( L_{P5} \frac{\partial \overline{\widetilde{T}}^{*}(x^{*}, z^{*})}{\partial z^{*}} \right) + \frac{\partial}{\partial x^{*}} \left( L_{P5} \frac{\partial \overline{\widetilde{T}}^{*}(x^{*}, z^{*})}{\partial x^{*}} \right) + \widetilde{T}_{MConvX} + \widetilde{T}_{MConvZ} + \widetilde{T}_{MSurfX} + \widetilde{T}_{MSurfZ} + \widetilde{T}_{MExchange}$$

#### **ENERGY EQUATION IN THE SOLID PHASE**

$$\frac{\partial}{\partial x^*} \left( L_{P7} \frac{\partial T_s^*(x^*, z^*)}{\partial x^*} \right) + \frac{\partial}{\partial z^*} \left( L_{P7} \frac{\partial T_s^*(x^*, z^*)}{\partial z^*} \right) + T_s^*_{MSurfX} + T_s^*_{MSurfZ} + T_s^*_{MExchange} = 0$$

## **Examples of Control Terms**

$$U_{MConv}\left(\hat{u},\hat{w},\partial S_{w},\Delta\Omega_{f},\Delta\Omega_{s}\right) = \frac{\partial}{\partial z}\left(\left\langle-\hat{u}\hat{w}\right\rangle_{f}\right) \qquad U_{MFriction}\left(U,\partial S_{w},v\right) = \frac{v}{\Delta\Omega}\int_{S_{w}}\frac{\partial U}{\partial x_{i}}d\bar{s}$$

$$U_{MDrag}\left(p,\partial S_{w}\right) = \frac{v}{\rho_{f}\Delta\Omega}\int_{S_{w}}pd\bar{s}$$

$$T_{fMConvX}\left(\hat{u},\hat{r}_{f},\Delta\Omega_{f},\Delta\Omega_{s}\right) = c_{pf}\rho_{f}\frac{\partial}{\partial x}\left(\left\langle m\right\rangle\left\{-\hat{r}_{f}\hat{u}\right\}_{f}\right) \qquad T_{fMConvZ}\left(\hat{w},\hat{T}_{f},\Delta\Omega_{f},\Delta\Omega_{s}\right) = c_{pf}\rho_{f}\frac{\partial}{\partial z}\left(\left\langle m\right\rangle\left\{-\hat{T}_{f}\hat{w}\right\}_{f}\right)$$

$$T_{fMSurfX}\left(k,T_{f},\partial S_{w}\right) = k\frac{\partial}{\partial x}\left[\frac{1}{\Delta\Omega}\int_{S_{w}}T_{f}d\bar{s}\right] \qquad T_{fMSurfZ}\left(k,T_{f},\partial S_{w}\right) = k\frac{\partial}{\partial z}\left[\frac{1}{\Delta\Omega}\int_{S_{w}}T_{f}d\bar{s}\right]$$

$$T_{fMExchange}\left(k,T_{f},\partial S_{w}\right) = k_{s}\frac{\partial}{\partial x}\left[\frac{1}{\Delta\Omega}\int_{S_{w}}T_{s}d\bar{s}_{I}\right] \qquad T_{sMSurfZ}\left(k_{s},T_{s},\partial S_{w}\right) = k_{s}\frac{\partial}{\partial z}\left[\frac{1}{\Delta\Omega}\int_{S_{w}}T_{s}d\bar{s}_{I}\right]$$

# **Optimization of Multiple Dimensional Cases** (6D Laminar or 8D Turbulent flow)

### **Use the statistical design of experiment (DOE) Methodology:**

- ! Choose an optimization variable; E  $_{Eff-het}$
- ! Systematically define the problem parameters and their ranges.
- ! Statistically analyze the numerical results to find the response surface.
- ! A commercial version of the DOE method was used to carry out the numerical simulation option.
- ! Choose the type of the response surface to be used and construct the response surface:

 $\dot{E_{ff}} = a_0 + a_1 X_1 + a_2 X_2 + \dots + a_n X_n + a_{11} X_1^2 + a_{12} X_1 X_2 + \dots + a_{nn} X_n^2$ 



### **Channel Flow Heat Transfer Optimization**

### **Example of Optimization of Simple Pin Fins**



## Fiber-optic LDV system overview



# **Experimental Test Apparatus**





### **Tested Heat Transfer Surfaces**



## **Experimental Investigation**

#### Comparison between numerical simulation and experiment.



 $E_{eff}(P_p)$ 

 $H_r(P_p)$ 



Heterogeneous effectiveness versus power for straight fin heat sink.

Heat transfer rate versus power for straight fin heat sink.



Comparison of Nu and  $f_f$  for heat sink experimental investigation



Heat sink heat transfer rate per unit volume per unit temperature difference



#### Heat sink conjugate wall Nusselt number



Heat sink friction factor



Heat sink heterogeneous and homogeneous effectiveness

# **Concluding Remarks**

#### Accomplishments:

- Constructed tunnel for augmented surface testing.
- Tested base case surfaces.
- Developed and demonstrated method for surface optimization.
- Selected initial geometric surface characteristics.
- Designed and tested new kind of heat sinks.